

Analysis of the data set of the rate constants

The rate constants of folding (k_f) can be related to the Gibbs free energies of activation, $\Delta G_f^{0\ddagger}$, using the transition state theory:

$$k_f = k^* \cdot \exp\left(-\frac{\Delta G_f^{0\ddagger}}{RT}\right) \quad (1)$$

The value of pre-exponential factor k^* represents the maximum rate for the folding reaction, which is assumed to be independent of both pressure (p) and the concentration of guanidine chloride ([GuHCl]). R is gas constant and T is temperature.

At constant temperature, $\Delta G_f^{0\ddagger}$ can be also represented with the activation volume ($\Delta V_f^{0\ddagger}$) as:

$$d\Delta G_f^{0\ddagger} = \Delta V_f^{0\ddagger} dp + m_f d[\text{GuHCl}] \quad (2)$$

where the m_f value represents the change in $\Delta G_f^{0\ddagger}$ with the [GuHCl] ($m_f = (\partial\Delta G_f^{0\ddagger}/\partial[\text{GuHCl}])_{p,T}$), which is empirically found to be constant over a wide range of GuHCl concentrations for protein folding reactions. To determine $\Delta G_f^{0\ddagger}$ at a certain p and [GuHCl], the effects of pressure and GuHCl on the m_f value and on $\Delta V_f^{0\ddagger}$ have to be taken into account. Because the differential of eq. (2) shows the following equation:

$$\frac{\partial^2 \Delta G_f^{0\ddagger}}{\partial p \partial [\text{GuHCl}]} = \left(\frac{m_f}{\partial p}\right)_{[\text{GuHCl}]} = \left(\frac{\partial \Delta V_f^{0\ddagger}}{\partial [\text{GuHCl}]}\right)_p = n_f \quad (3)$$

where n_f is the constant that is independent of both pressure and denaturant concentration, the integration of eq. (2) gives:

$$\ln k_f(p, [\text{GuHCl}]) = \ln k_f(p_0, [\text{GuHCl}]_0) - \frac{\Delta V_f^{0\ddagger}([\text{GuHCl}])}{RT} \cdot (p - p_0) - \frac{m_f(p_0)}{RT} \cdot [\text{GuHCl}] \quad (4)$$

$$\Delta V_f^{0\ddagger}([\text{GuHCl}]) = \Delta V_f^{0\ddagger}([\text{GuHCl}]_0) + n_f \cdot [\text{GuHCl}] \quad (5)$$

where $k_f(p, [\text{GuHCl}])$ is the folding rate at p and [GuHCl] and $k_f(p_0, [\text{GuHCl}]_0)$ is the folding rate at ambient pressure (0.1 MPa) and in the absence of GuHCl. $m_f(p_0)$ is the m_f value at ambient pressure. $\Delta V_f^{0\ddagger}([\text{GuHCl}]_0)$ is the activation volume in the absence of GuHCl.

The validity of the linear dependence of the activation volumes on the concentration of GuHCl can be assessed by eq. (3). Based on the pressure dependence of the m_f -values, the n_f -value was estimated to be $6.3 \pm 2.4 \text{ cm}^3 \cdot \text{mol}^{-1} \cdot \text{M}^{-1}$, while the GuHCl concentration dependence of the activation volumes showed that the n_f -value is $6.3 \pm 2.0 \text{ cm}^3 \cdot \text{mol}^{-1} \cdot \text{M}^{-1}$. Such coincidence in the n_f -values clearly indicates that the assumption of the linear fitting of the activation volume against the GuHCl concentration with eq. (5) is reasonable.

The data set of the rate constants determined at high pressure p and [GuHCl] can be, therefore, globally fitted with eqs. (4) and (5). The parameters; $k_f(p_0, [\text{GuHCl}]_0)$, $m_f(p_0)$, and $\Delta V_f^{0\ddagger}([\text{GuHCl}]_0)$ were estimated to be

$11.9 \pm 0.9 \times 10^3 \text{ s}^{-1}$, $5.8 \pm 0.3 \text{ kJ}\cdot\text{mol}^{-1}\cdot\text{M}^{-1}$, and $-15 \pm 7 \text{ cm}^3\cdot\text{mol}^{-1}$, respectively. By using the data set of the kinetic measurements at ambient pressure, $k_f(p_0, [\text{GuHCl}]_0)$ and $m_f(p_0)$ were also calculated to be $12.1 \pm 0.8 \times 10^3 \text{ s}^{-1}$ and $5.3 \pm 0.4 \text{ kJ}\cdot\text{mol}^{-1}\cdot\text{M}^{-1}$, respectively, both of which are virtually the same as those from the high pressure measurements (10-200 MPa) ($11.9 \pm 0.9 \times 10^3 \text{ s}^{-1}$ and $5.8 \pm 0.3 \text{ kJ}\cdot\text{mol}^{-1}\cdot\text{M}^{-1}$, respectively). The good agreement of kinetic parameters at ambient and high pressure demonstrates the reliability of the estimation of the activation volume in the absence of the denaturant at ambient pressure.